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SEMINAR NOTES: FILTER, THEORY, DESIGN AND APPLICATIONS, (U)  
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6 SEMINAR NOTES

FILTER, THEORY, DESIGN AND APPLICATIONS

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NOTES

A BASIC REVIEW OF FILTER THEORY

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## IDEAL FILTER

There are two ways of viewing the characteristics of an ideal filter. The first and most common is from the point of view of the frequency domain. This first class of filters would pass without attenuation all frequencies inside certain frequency limits and provide infinite attenuation for all other frequencies. The second point of view is from the time domain. A designer may only be interested in the time response of a filter. This class of filters would have an output that is identical to its input except be delayed by some time  $\tau_0$ .

This set of notes will present in a basic manner some of the characteristics of mathematical models which have been derived to approximate these two types of filters.

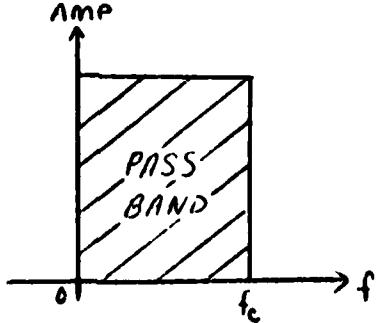
The first class of filters to be considered are those whose desired response is to pass or attenuate specific frequency ranges. We will discuss four basic types of filters in this class. These are Low-Pass, Band Pass, High Pass, and Bandreject.

Based on the definition of the ideal filter the following filter types can be defined.

### Low-Pass Filter

Passes signals from zero frequency up to a certain cutoff frequency and rejects all signals whose frequency is beyond the cutoff frequency.

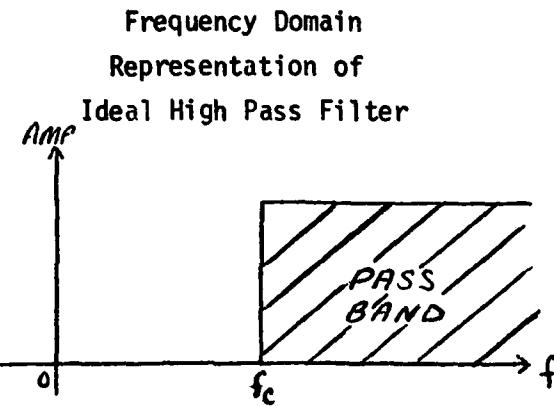
Frequency Domain  
Representation of  
Ideal Low-Pass Filter



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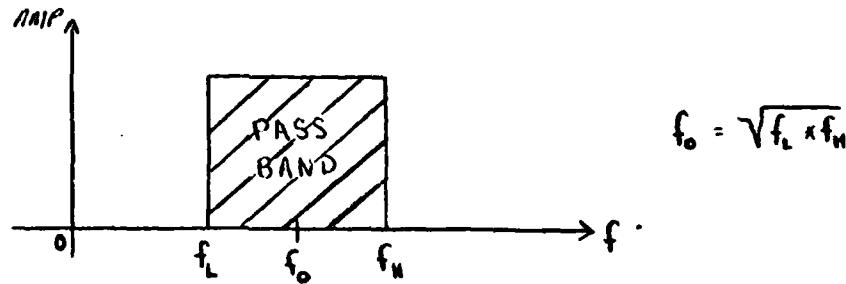
### High Pass Filter

Rejects all signals up to  $f_c$  and passes all frequencies greater than  $f_c$  with no attenuation.



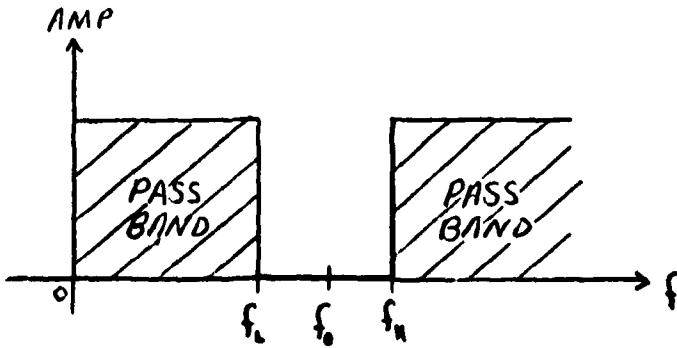
### Band Pass Filter

Passes only those signals that are within a specific frequency band and rejects all others.



### Bandreject Filter

Rejects those signals within a specific frequency band and passes all others.

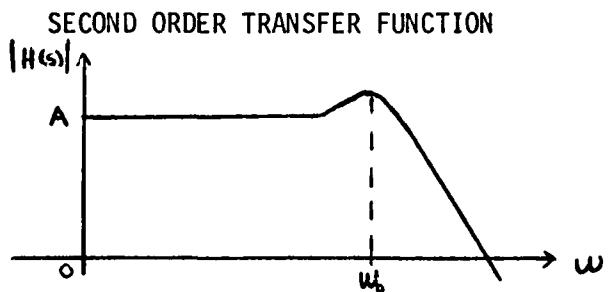


The shapes of these filters must be approximated by mathematical models which can be physically realized before a circuit can be built which will behave like the desired filter.

These mathematical models are based on the ratio of two polynomials in  $S$ . In order to develop a feel for the shape of the amplitude versus frequency curve of various polynomials in  $S$  let us consider one such function. We will discuss a second order function in order to keep the description simple and still deal with all of the basic parameters of an  $N$ th order function. The function we will consider is Equation 1.

$$(1) \quad H(s) = \frac{H_0}{s^2 + \frac{\omega_0 s}{Q} + \omega_0^2}$$

Figure 1 shows the magnitude of  $H(s)$  as a function of the real frequency ( $S = j\omega$ )  $\omega$ .



In general you can select values for the parameters  $H_0$ ,  $\omega_0$ , and  $Q$  and you will have slightly different amplitude vs frequency plots. There is, however, one characteristic which will not change. That is, as the frequency  $\omega$  gets far away from  $\omega_0$  the roll off (slope of the curve) becomes  $-N \cdot 20 \text{ dB/decade}$  where  $N$  is the order of the filter. In this case  $N = 2$  and the slope is  $-40 \text{ dB/decade}$ .

It is generally desired to have the gain at  $\omega = 0$  (i.e.  $A$ ) be set to 1. Let's look at the result of this criteria.

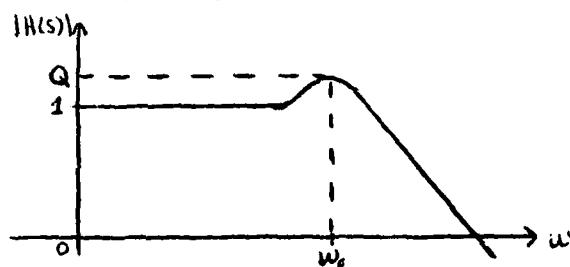
$$A = H(j\omega) = \frac{H_0}{(j\omega)^2 + \frac{\omega_0}{Q}(j\omega) + \omega_0^2} = \frac{H_0}{\omega_0^2}$$

$$A = 1 = \frac{H_0}{\omega_0^2}$$

Solve for  $H_0$

$$H_0 = \omega_0^2$$

The result is the following general transfer function.



We call  $\omega_0$  the corner frequency. Let's find the magnitude of  $H(s)$  at  $\omega = \omega_0$ .

$$H(j\omega_0) = \frac{\omega_0^2}{(j\omega_0)^2 + \frac{\omega_0}{Q}(j\omega_0) + \omega_0^2} = \frac{\omega_0^2}{-\omega_0^2 + j\frac{\omega_0}{Q} + \omega_0^2}$$

$$H(j\omega_0) = \frac{\omega_0^2}{j\frac{\omega_0^2}{Q}} = Q \quad \boxed{-90^\circ}$$

Thus we see that the magnitude of the transfer function at  $\omega_0 = Q$ .

NOTICE: A potential hardware implementation problem can come about with high Q circuits.

Example:

Requirement: DC gain = 1 (i.e.  $|H(j\omega)|$  at  $\omega = 0$  is 1)

$$\omega_0 = 1 \text{ KHz}$$

$$Q = 10$$

Max. Input Voltage  
Swing =  $\pm 10$  volts

NOTICE: At  $\omega_0$  (1 KHz) the filter gain will be 10 (Q).

This requires that the output be capable of swinging  $\pm 100$  volts.

You can get around this by making  $H_0 = \frac{\omega_0^2}{Q}$

In actuality a customer would not specify a Q for the filter but instead he will have a desired shape for the transfer function. The shape is controlled by the location of the poles and zeros of the transfer function.

The poles of the function are the values of S ( $j\omega$ ) which make the denominator zero. The zeros of the function are the values of S( $j\omega$ ) which make the numerator zero.

For the 2 pole low pass transfer function there are 2 poles (obviously).

$$s_1 = -\frac{\omega_0}{2Q} + j\omega_0 \sqrt{1 - \frac{1}{4Q^2}}$$

$$s_2 = -\frac{\omega_0}{2Q} - j\omega_0 \sqrt{1 - \frac{1}{4Q^2}}$$

and two zeros

$$s = +\infty$$

$$s = -\infty$$

By changing the location of the poles of this function you can change the shape of the function.

Let's say you wanted to stretch out the function i.e. move  $\omega_0$ . To do this all you have to do is to multiply all the poles by a constant K where K is the ratio of the new corner frequency  $\omega$  to the original frequency  $\omega_0$  (i.e.  $K = \frac{\omega}{\omega_0}$ ).

EXAMPLE: Given the general pole values

$$s_{p1} = -\alpha + jB$$

$$s_{p2} = -\alpha - jB$$

The frequency shifted poles would be

$$s_{p1}^* = -K\alpha + jKB$$

$$s_{p2}^* = -K\alpha - jKB$$

If you multiply out the poles and compare them with the original denominator of  $H(s)$  you will find that your scaled transfer function is now

$$H(s)^* = \frac{\omega_0^2}{s^2 + K\omega_0 s + K^2\omega_0^2}$$

Changing the poles by changing  $\alpha$  and/or B will effect the shape of the transfer function. Let's look at the general transfer function and compare it to the expansion of the two general pole equations.

$$s_1 = -\alpha + jB \quad s_2 = -\alpha - jB$$

multiplying these poles together

$$(s + \alpha - jB)(s + \alpha + jB) = s^2 + 2\alpha s + (\alpha^2 + B^2)$$

Comparing co-efficients of S with the original transfer function we see that

$$\omega_0 = \sqrt{\alpha^2 + B^2}$$

and

$$Q = \frac{\omega_0}{2\alpha}$$

We can thus see that by changing  $\alpha$  and/or  $B$  we can change  $\omega_0$  and/or  $Q$ . It is not immediately clear from these equations how the shape of the function will change by a change in pole location.

There are equations which will tell us where to put the poles of a transfer function in order to achieve a certain shape. That is where Tchebyscheff, Butterworth and Bessel and numerous other mathematicians come into the act.

Before we get to them let's take a second to note what the location of the zeros of the functions do to its shape.

Lets move one of those zeros that is out at  $\infty$  and bring it in to  $\omega=0$ . The result is:

$$H(s) = \frac{SH_0}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$$

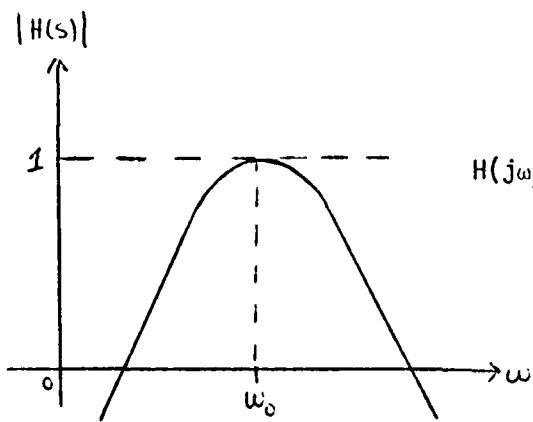
Note at  $s=0$  the function is 0

and at  $s=\infty$  the function is 0

and we can show by taking a derivative  
that the function is a maximum at

$$s=j\omega_0$$

The result is a shape as shown below.



Let's solve for  $|H(j\omega_0)|$

$$H(j\omega_0) = \frac{H_0 j\omega_0}{(j\omega_0)^2 + \frac{\omega_0}{Q}(j\omega_0) + \omega_0^2}$$

$$= \frac{j H_0 \omega_0}{j \frac{\omega_0^2}{Q}}$$

$$= \frac{H_0 \omega_0 Q}{\omega_0^2}$$

$$|H(j\omega_0)| = \frac{H_0 Q}{\omega_0}$$

If we set the gain at the center = 1

we have

$$H_0 = \frac{\omega_0}{Q}$$

We thus have the general transfer function for a second order Bandpass filter

$$H(S) = \frac{H_0 S}{S^2 + \frac{\omega_0}{Q} S + \omega_0^2}$$

If we move both zeros from  $\infty$  to 0 we have a transfer function as follows

$$H(S) = \frac{H_0 S^2}{S^2 + \frac{\omega_0}{Q} S + \omega_0^2}$$

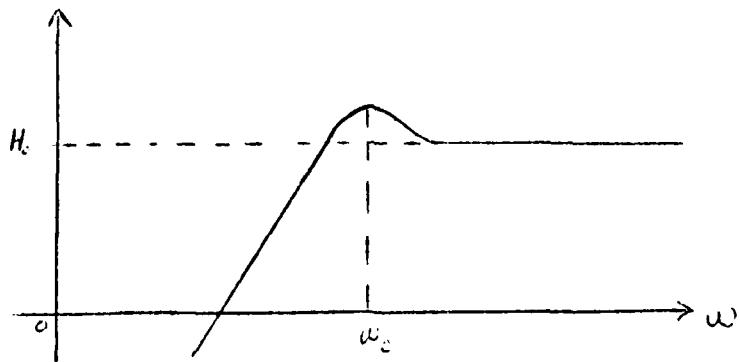
Notice: The value at  $S=0$  is 0

The value at  $S=\infty$  is  $H_0$

(divide numerator and denominator by  $S^2$  and let  $S \rightarrow \infty$ )

The shape of this is a highpass function

$$|H(j\omega)|$$



Thus by moving the zeros of the transfer function we can generate lowpass, highpass, bandpass or even band reject filters if we place both zeros at the frequency we want to reject.

Since we can derive any type filter depending only on zero locations we will now talk only about the lowpass filter poles realizing that the same general characteristics will hold true for the other filter types.

One desirable transfer function shape is one which is maximally flat in the passband.

A Butterworth filter has this characteristic. The pole locations for a Butterworth filter are given by the following equations.

#### Butterworth Formulas

$$N = \text{Degree of filter} = \# \text{ of poles}$$

Attenuation ratio

$$A = \sqrt{1 + \omega^2 N}$$

$$\alpha = 20 \log A$$

Note: All filters in Butterworth family have 3dB at  $\omega=1$ .

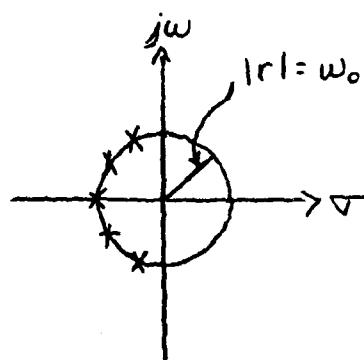
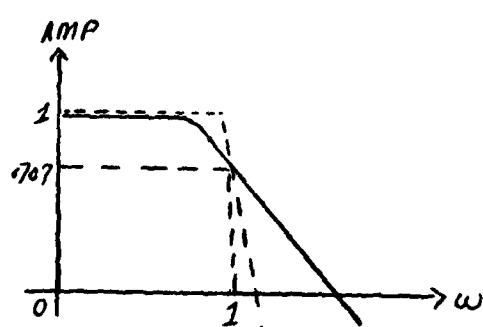
Pole location

Poles from  $K=1$  to  $N$

$$P_K = -\sin \theta_K + j \cos \theta_K$$

$$\theta_K = \frac{(2K-1)\pi}{2N} = (2K-1) \frac{90^\circ}{N}$$

Note  $P_{N-K+1}$  is Complex conjugate of  $P_K$



When you think of a filter most often you think of the ideal case with an infinitely steep roll off. Because of certain physical constraints we cannot achieve  $\sim \text{dB}/\text{decade}$  but a Tchebyscheff type filter tends to give maximum roll off with a small sacrifice in the flatness in the passband.

TCHEBYSCHEFF -- Very fast initial roll off  
 final roll off  $-N*20\text{dB}/\text{decade}$   
 $-N*6\text{dB}/\text{octave}$

#### Attenuation Ratio

$$A(\omega) = \sqrt{1 + \epsilon^2 C_N^2(\omega)}$$

Given  $\alpha_0$  in dB  $\leftarrow$  Passband Ripple

$$\epsilon = \sqrt{10^{\frac{1}{20} \alpha_0} - 1}$$

$C_N(\omega)$  - Tchebyscheff Polynomials  
 for  $\omega > 1$  i.e. stop band

\*  $C_N(\omega) = \text{Cosh}(N \text{ Cosh}^{-1} \omega)$

or solving for  $\omega$

$$\omega = \text{Cosh}\left(\frac{1}{N} \text{Cosh}^{-1} C_N(\omega)\right)$$

for  $\omega < 1$  in passband

\*  $C_N(\omega) = \text{Cos}(N \text{ Cos}^{-1} \omega)$

or

$$\omega = \text{Cos}\left(\frac{1}{N} \text{Cos}^{-1} C_N(\omega)\right)$$

Tchebyscheff Polynomials  $C_N(\omega)$

$N$	$C_N(\omega)$
1	$\omega$
2	$2\omega^2 - 1$
3	$4\omega^3 - 3\omega$
4	$8\omega^4 - 8\omega^2 + 1$
5	$16\omega^5 - 20\omega^3 + 5\omega$

## Tchebyscheff Poles

for  $K=1 \rightarrow N$  poles

$$P_K = -\sin \theta_K \sinh \beta + j \cos \theta_K \cosh \beta$$

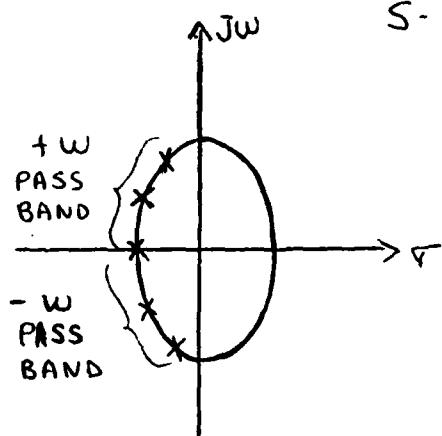
$$\text{where } \theta_K = (2K-1) \frac{\pi}{2N} = (2K-1) \frac{90^\circ}{N}$$

$$\beta = \frac{1}{N} \sinh^{-1} \left( \frac{1}{e} \right)$$

Note:  $P_{N-K+1}$  &  $P_K$  are complex conjugates  
When  $N$  is odd there is one real pole

$$\frac{P_{N+1}}{2} = -\sinh \beta$$

S-plane plot



## Refresher Equations

$$\sinh x = \frac{e^x - e^{-x}}{2} = \frac{(e^x + e^{-x})}{2} \cdot \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{(e^x + e^{-x})}{2} \cdot \frac{1 - e^{-2x}}{1 + e^{-2x}}$$

$$\cosh x = \frac{e^x + e^{-x}}{2} = \frac{(e^x + e^{-x})}{2} \cdot \frac{1 + e^{-2x}}{1 + e^{-2x}} = \frac{(e^x + e^{-x})}{2} \cdot \frac{1 + e^{-2x}}{1 + e^{-2x}}$$

$$\sinh^{-1} x = \ln (x + \sqrt{x^2 + 1})$$

$$\cosh^{-1} x = \ln (x + \sqrt{x^2 - 1})$$

Useful identity to generate table

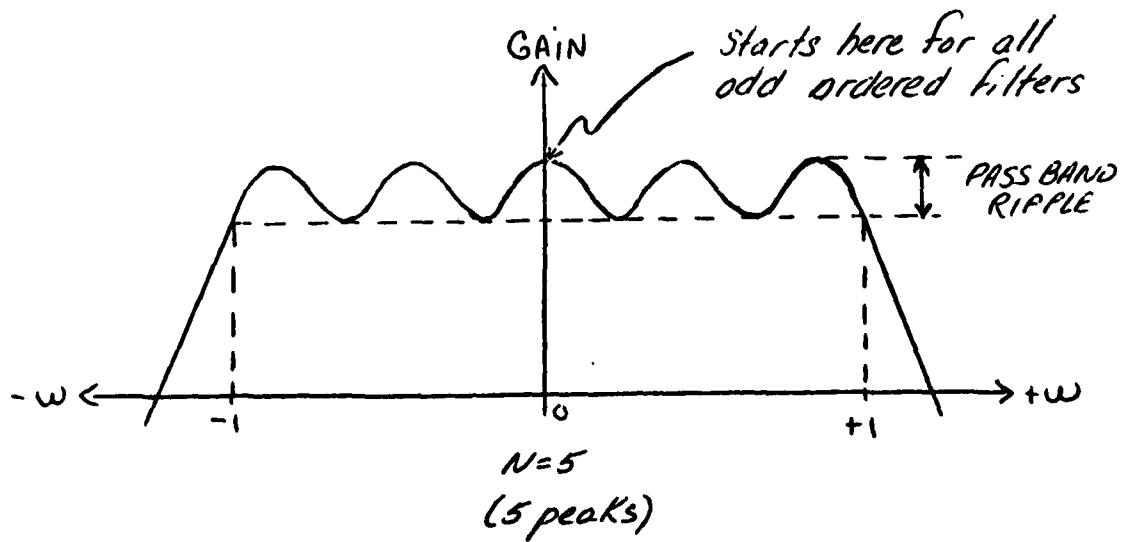
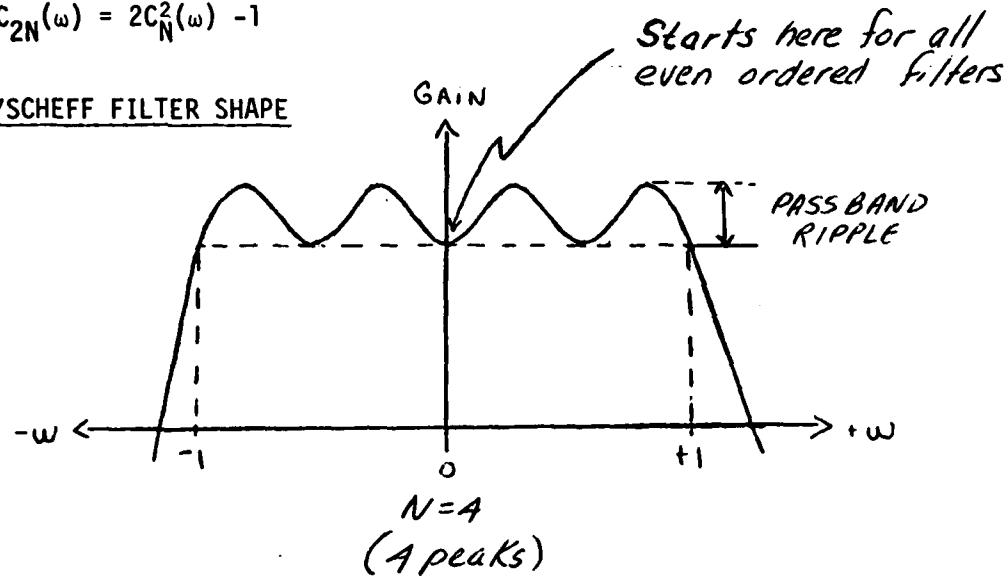
$$C_N(\omega) = 2\omega C_{N-1}(\omega) - C_{N-2}(\omega)$$

Useful identity when evaluating  $A(\omega)$

$$C_N^2(\omega) = \sqrt{C_{2N}(\omega) + 1}$$

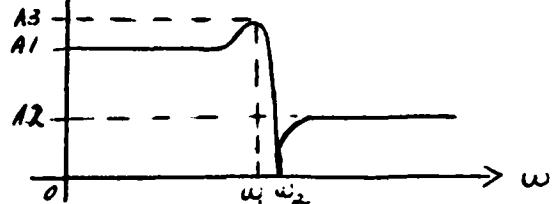
$$C_{2N}(\omega) = 2C_N^2(\omega) - 1$$

#### TCHEBYSCHEFF FILTER SHAPE



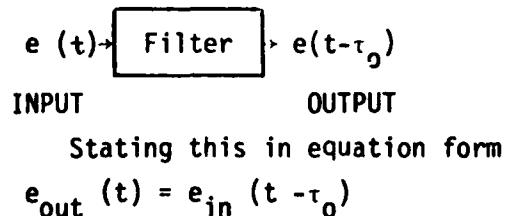
A third filter type which sacrifices attenuation in the stopband for rapid roll off is the Elliptic filter. Its transfer function is formed by placing the zeros near the poles of the function rather than at the two extremes of the frequency spectrum. A typical transfer function is shown below:  $\uparrow |H(j\omega)|$

$$H(S) = \frac{H_0 (S^2 + a)}{S^2 + \omega_0^2}$$



A very steep roll off can be achieved with this type filter as long as the resultant floor of attenuation A2 can be tolerated. Notice that as you bring the zero in from  $\infty$  the roll off increases and so does the floor. When the zero is located at the corner frequency (assuming originally we had a Butterworth transfer function) the result is a Band Reject filter.

Let's now consider the class of filters that attempt to satisfy the time domain condition of pure time delay. Mathematically the transfer function must be as follows:



We must now see what this equation looks like in the frequency domain ( $S$ ).

Let's take the Laplace transform of both sides of this equation.

Starting with  $e_{out}(t)$

$$\mathcal{L}[f(t)] = \int_0^{\infty} f(t) e^{-st} dt = F(s)$$

$$\mathcal{L} [e_{\text{out}}(t)] = \int_0^{\infty} e_{\text{out}}(t) e^{-st} dt = E_0(s)$$

Now with the Rt side

$$\mathcal{L}[e_{in}(t - \tau_0)] = \int_0^{\infty} e_{in}(t - \tau_0) e^{-st} dt$$

make a variable substitution  $t^* = t - \tau_0$

then  $dt^* = dt$  &  $t = t^* + \tau_0$

$$= \int_0^\infty e_{in}(t^*) e^{-s(t^* + \tau_0)} dt^*$$

$$= \int_0^\infty e_{in}(t^*) e^{-st^*} e^{-s\tau_0} dt^*$$

Note  $e^{-s\tau_0}$  is a constant over the integral so

$$= e^{-s\tau_0} \int_0^\infty e_{in}(t^*) e^{-st^*} dt^* \quad \text{let } t = t^* \text{ and we see}$$

$$\mathcal{L}[e_{in}(t - \tau_0)] = e^{-s\tau_0} E_{in}(s)$$

Now forming the original equation we have

$$E_{out}(s) = e^{-s\tau_0} E_{in}(s)$$

$$\frac{E_{out}(s)}{E_{in}(s)} = e^{-s\tau_0}$$

$$H(s) = e^{-s\tau_0}$$

$H(s)$  is the frequency domain equivalent of the original time domain transfer function.

There are two important characteristics of  $H(s)^*$

- 1) Its amplitude is 1 i.e. independent of frequency
- 2) Its phase is proportional to frequency with proportionality constant  $\tau_0$ .

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\* Recall  $S = j\omega$  Therefore  $H(j\omega) = e^{-j\omega\tau_0}$ ; from Eulers identity

$e^{-j\omega\tau_0} = \cos \omega \tau_0 - j \sin \omega \tau_0$ . The amplitude of this complex number is  $\sqrt{(\cos \omega \tau_0)^2 + (\sin \omega \tau_0)^2} = \sqrt{1} = 1$ . Its phase angle is

$$\arctan \frac{-\sin \omega \tau_0}{\cos \omega \tau_0} = \arctan (-\tan \omega \tau_0) = -\omega \tau_0$$

A Bessel type filter approximates this desired response for input signals within a specified passband.

$$H(S) = \frac{H_0}{B_n(S)}$$

where

$$B_n(S) = a_0 + a_1 S + \dots + a_{n-1} S^{n-1} + S^n$$

where the coefficients  $a_i$  are computed from the following equation

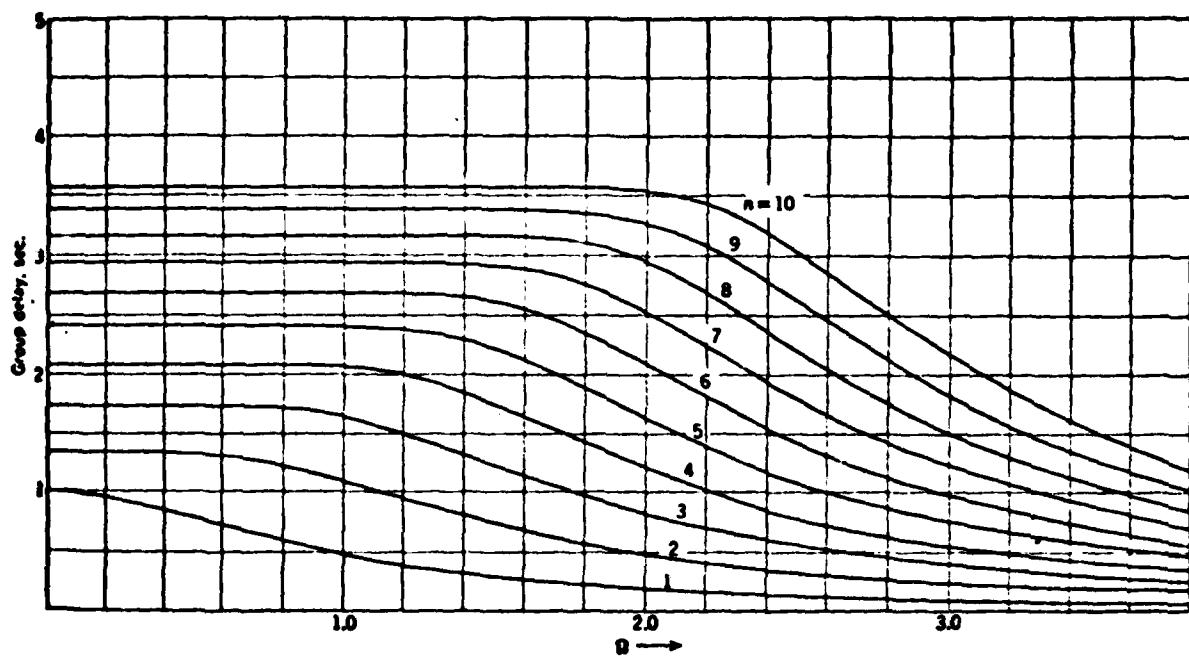
$$a_i = \frac{(2n-i)!}{i!(n-i)!} (2\tau_0)^{i-n} \text{ for } i=0,1,2,\dots,n-1$$

$n$  = the order of the filter

$\tau_0$  = delay time

The corner of the Bessel filter is generally specified as  $\omega = \frac{1}{\tau_0}$ . F.D.I. specifies it as the -3dB point in order to keep all of our specifications consistent. Note the F.D.I. corner is just  $K \cdot \frac{1}{\tau_0}$ . A good measure of the linearity of the phase across the passband is the term called the Group Delay. The Group Delay is the derivative of the phase. If the group delay is a constant then the phase will be linear. The Bessel coefficients are derived by establishing a criteria of maximally flat group delay.

Over the passband the phase increases linearly from 0 to  $n\pi/4$  radians at the cut off frequency.



Group-delay characteristics for maximally flat delay (Bessel) filters.

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Inc. New York

NOTES

IMPLEMENTATION OF THE FILTER THEORY

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## IMPLEMENTATION OF FILTER THEORY

### Topical Outline

1. Two types of filter synthesis commonly used to realize filter polynominal functions

- A. Passive RLC ladder synthesis techniques
- B. Active RC and Amplifier techniques

2. Design techniques that simply design procedures for passive and active filters

- A. Frequency scaling
- B. Impedance scaling
- C. Lowpass to Bandpass and other transformation

$$\text{LP - BP} \quad S \rightarrow \frac{S^2 + \omega_0^2}{S}$$

gives Geometric Symmetry

$$\text{LP - HP} \quad S \rightarrow \frac{1}{S}$$

3. Design Lowpass filters and transform up to  $\omega_0$  to get Bandpass filters

4. Circuit Configurations

- A. Stagger tuned
- B. Leap frog
- C. Primary resonator block
- D. Analog computer circuit

5. Some common active filter circuits

- A. Sallen and key resonator
- B. Multiple feedback
- C. State variable - dual integrator

6. Sensitivities of various circuit configurations

7. Practical limitations for active filters

- A. Q is limited by available gain
- B. DC offset and noise of amplifiers
- C. Frequency limitations (QA product)

**NOTES**

**FILTER SPECIFICATIONS**

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## ABSTRACT

The Active Filter is now available in what is commonly referred to as component form. It is an item the system designer may order off the shelf in any of a variety of configurations. As is the case with any component there are performance limitations to be considered and benefits to be derived by proper selection and application.

The presentation will outline system factors which relate directly to filter selection and review the state of the art from a performance point of view. Individual filter specifications will be discussed. The importance and method defining the filtering requirements before selecting a filter type will be emphasized.

FILTER SPECIFICATIONS

(typical @ 25°C and  $\pm 15V$  unless otherwise specified)

	REQUIRED	DESIRED	TYPICAL
Center/Cutoff Frequency	_____	_____	.001 to 50kHz
Tuning Range	_____	_____	20:1 to 1000:1
Drift	_____	_____	50 to 100 ppm/°C
Tolerance (Fixed Frequency)	_____	_____	to $\pm .1\%$
Passband Gain	_____	_____	0 to 60dB
Amplitude Match	_____	_____	Match is a Function of the sensitivity & initial tolerance of the design to be used
Frequency Range	_____	_____	
Phase Match	_____	_____	
Frequency Range	_____	_____	
Input			
Impedance	_____	_____	$10^3$ to $10^9\Omega$
Source	_____	_____	typ $<600\Omega$
Bias Current	_____	_____	1-10mA
Voltage Range	_____	_____	$\pm 10V$ at $\pm 15V$ $V_s$
Safe Input Voltage	_____	_____	$V_s$
Output			
Full Power Response	_____	_____	50kHz
Noise	_____	_____	10 to $50\mu V$
Rated Output	_____	_____	2-5mA
Offset Voltage	_____	_____	1mV-10mV
Drift	_____	_____	10 to $20\mu V/^\circ C$
Resistance	_____	_____	1Ω to 10Ω
Power Requirements			
Quiescent Current (mA)	_____	_____	Depends on Device
Voltage, Rated Specs (V)	_____	_____	$\pm 15V$
Voltage, Operating	_____	_____	$\pm 5$ to $\pm 18V$
Temperature (°C)			
Commercial Operating	_____	_____	0 to 70
Storage	_____	_____	-25 to +85 ( $-55$ to +125)
Military Operating	_____	_____	-25 to +85 (-55 to +125)
Storage	_____	_____	-65 to 150
Standard Mechanical Configurations			
Length	_____	_____	1.0" to 3.00"
Width	_____	_____	1.0" to 2.00"
Height	_____	_____	0.4" to 1.00"

### DEFINITION OF VARIABLES:

#### FIGURE 1 & 2

**NOISE:** Maximum acceptable level should be indicated.

**RIPPLE:** Acceptable variation in passband gain

**GAIN:** Desired passband gain @  $f_o$

#### FIGURE 1:

$f_{R1}, f_{R2}$  : Limits of ripple band

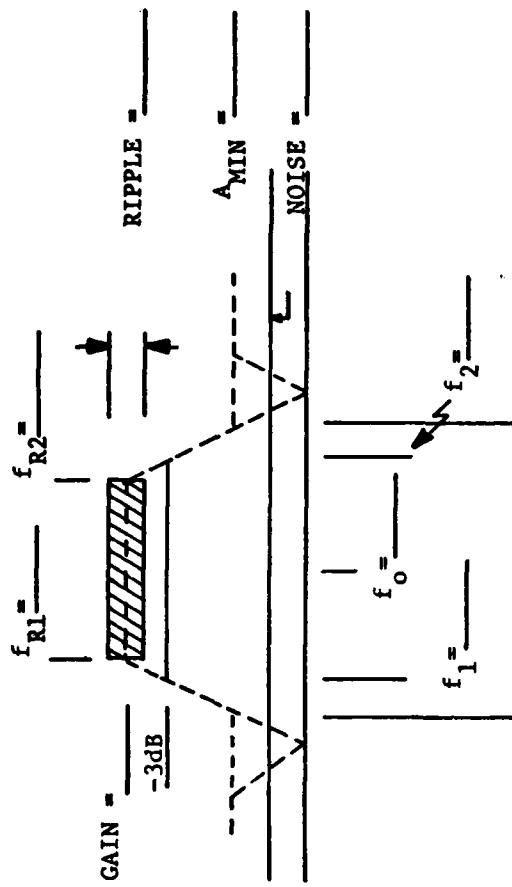
$f_1, f_2$  : -3dB Attenuation frequencies

$f_o = \sqrt{f_1 f_2}$  : Center frequency

$A_{\min}$  : Minimum stopband attenuation, if monotonic roll off is required this must be specified.

$f_{A1}, f_{A2}$  : Frequencies by which a given attenuation  $A_{\min}$  must be achieved.

FIGURE 1: Bandpass



#### FIGURE 2:

$f_{R1}, f_{R2}$  : Limits of the ripple band

$f_{\max}$  : Maximum frequency at which full power response is required

$f_o = \sqrt{f_1 f_2}$  : Center frequency

$f_{A1}, f_{A2}$  : Limits of Attenuation Band (stopband)

$A_{\min}$  : Required Stopband Attenuation to be maintained  $f < f_{A1}$  and/or  $f > f_{A2}$

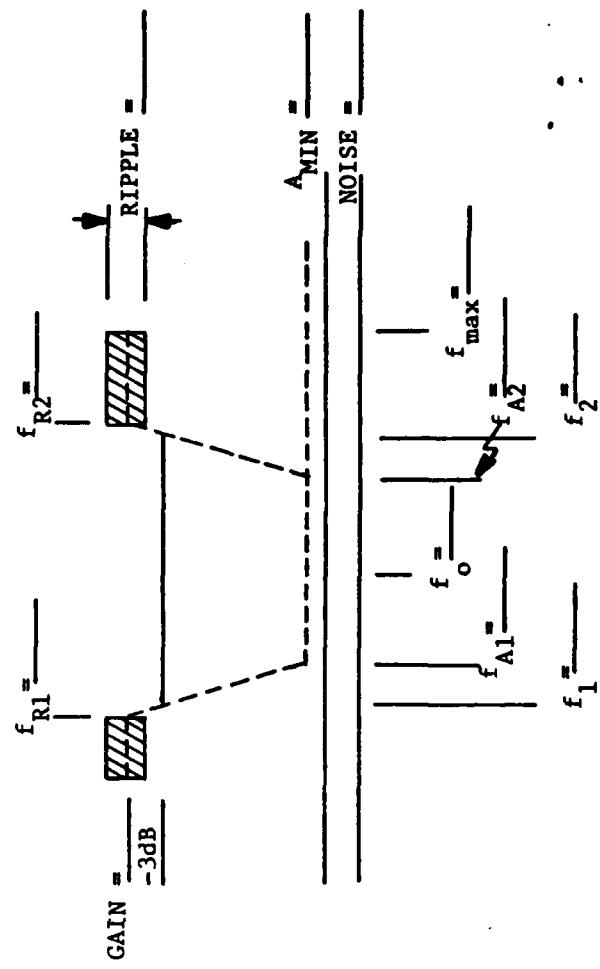
#### For Lowpass:

$f_1 = f_c = -3\text{dB}$  or cutoff frequency  
 $A_{\min}, f_{A1}$ , as described above

#### For Highpass:

$f_2 = f_c = -3\text{dB}$  or cutoff frequency  
 $A_{\min}, f_{A2}$ , as described above

FIGURE 2: Band Reject, Highpass, Lowpass



FILTER SPECIFICATIONS

(typical @ 25°C and  $\pm 15V$  unless otherwise specified)

	REQUIRED	DESIRED	TYPICAL
Center/Cutoff Frequency	_____	_____	.001 to 50kHz
Tuning Range	_____	_____	20:1 to 1000:1
Drift	_____	_____	50 to 100 ppm/°C
Tolerance (Fixed Frequency)	_____	_____	to $\pm .1\%$
Passband Gain	_____	_____	0 to 60dB
Amplitude Match	_____	_____	Match is a Function of the sensitivity & initial tolerance of the design to be used
Frequency Range	_____	_____	
Phase Match	_____	_____	
Frequency Range	_____	_____	
Input			
Impedance	_____	_____	$10^3$ to $10^9\Omega$
Source	_____	_____	typ $<600\Omega$
Bias Current	_____	_____	1-10nA
Voltage Range	_____	_____	$\pm 10V$ at $\pm 15V V_s$
Safe Input Voltage	_____	_____	$V_s$
Output			
Full Power Response	_____	_____	50kHz
Noise	_____	_____	10 to $50\mu V$
Rated Output	_____	_____	2-5mA
Offset Voltage	_____	_____	1mV-10mV
Drift	_____	_____	10 to $20\mu V/^\circ C$
Resistance	_____	_____	$1\Omega$ to $10\Omega$
Power Requirements			
Quiescent Current (mA)	_____	_____	Depends on Device
Voltage, Rated Specs (V)	_____	_____	$\pm 15V$
Voltage, Operating	_____	_____	$\pm 5$ to $\pm 18V$
Temperature (°C)			
Commercial Operating	_____	_____	0 to 70
Storage	_____	_____	-25 to +85 (-55 to +125)
Military Operating	_____	_____	-25 to +85 (-55 to +125)
Storage	_____	_____	-65 to 150
Standard Mechanical Configurations			
Length	_____	_____	1.0" to 3.00"
Width	_____	_____	1.0" to 2.00"
Height	_____	_____	0.4" to 1.00"

#### DEFINITION OF VARIABLES:

FIGURE 1 & 2

NOISE: Maximum acceptable level should be indicated.

RIPPLE:

Acceptable variation in passband gain  
Desired passband gain @  $f_o$

FIGURE 1:

$f_{R1}, f_{R2}$  : Limits of ripple band  
 $f_1, f_2$  : -3dB Attenuation frequencies  
 $f_o = \sqrt{f_1 f_2}$  : Center frequency  
 $A_{min}$  : Minimum stopband attenuation, if monotonic roll off is required this must be specified.

$f_{A1}, f_{A2}$  : Frequencies by which a given attenuation  $A_{min}$  must be achieved.

FIGURE 1: Bandpass

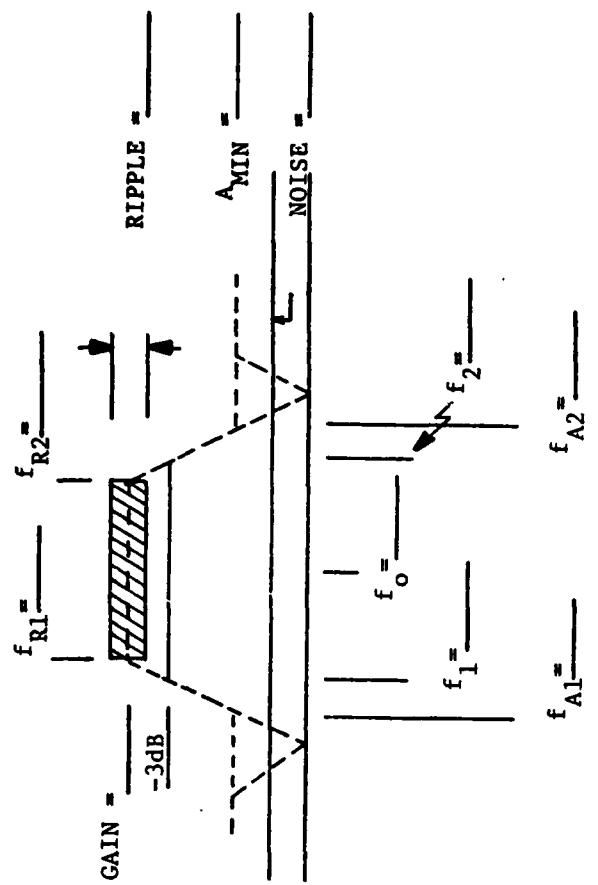


FIGURE 2:

$f_{R1}, f_{R2}$  : Limits of the ripple band  
 $f_{max}$  : Maximum frequency at which full power response is required  
 $f_o = \sqrt{f_1 f_2}$  : Center frequency  
 $f_{A1}, f_{A2}$  : Limits of Attenuation Band (stopband)  
 $A_{min}$  : Required Stopband Attenuation to be maintained  $f > f_{A1}$  and/or  $f < f_{A2}$

For Lowpass:

$f_1 = f_c = -3\text{dB}$  or cutoff frequency  
 $A_{min}, f_{A1}$ , as described above

For Highpass:

$f_2 = f_c = -3\text{dB}$  or cutoff frequency  
 $A_{min}, f_{A2}$  as described above

FIGURE 2: Band Reject, Highpass, Lowpass

